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## GIT and the moduli of curves

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Abstract: I will discuss some recent progress made by Hassett and Hyeon on the moduli space of curves of genus g. Their work revolves around the study of the stability in the sense of Geometric Invariant Theory of *n*-canonical embeddings of smooth curves and the corresponding compactifications of the moduli space. For  $n \ge 5$ , it has been long known that this compactification is the Deligne-Mumford compactification. Schubert studied the cases when n is three or four. For n = 2, the Hilbert stability compactification is related to Schubert's compactification by a flip through the Chow stability compactification. These compactifications turn out to be log canonical models for  $(\bar{M}_q, \alpha \delta)$  for  $\alpha$  near 7/10.